

Implementing formative assessment in the context of algebra

Dietmar Küchemann, Jeremy Hodgen, Margaret Brown

King's College London, London, United Kingdom

Background

There is good evidence to suggest the efficacy of an approach based on formative assessment and feedback (Black & William, 1998; Hattie & Timperley, 2007). In England, over the past decade formative assessment has been phenomenally “successful” with both policy-makers and the teaching profession. Much of this influence is due to a developmental research project conducted partly in secondary mathematics (Black et al, 2003). Yet, evidence suggests that teachers and schools have considerable difficulties in implementing the approach (e.g., Smith & Gorard, 2005), particularly in mathematics (PricewaterhouseCoopers, 2008). There are several reasons for these difficulties. First, although much of the evidence relating to the efficacy of formative assessment is situated in mathematics education contexts, to date, descriptions of the approach have largely focused on a generic pedagogy rather than on subject-specific didactics. Teachers’ ability to use formative assessment and feedback in mathematics is limited by their knowledge about key mathematical ideas, the likely difficulties that students will face, and appropriate pedagogic strategies. Thus, if teachers focus on teaching mathematical procedures, they may find it difficult to see the causes of problems for students in mastering and applying these, and though aware of the importance of particular generic formative assessment strategies (e.g. questioning or facilitating dialogue), they may not know how to implement these strategies mathematically nor how to tailor them to the particular learning needs of their students (Hodgen, 2007; Watson, 2006). Current textbooks in England accentuate the problem by presenting school mathematics as fragmentary and lacking coherence (Haggarty and Pepin, 2001). Second, interventions associated with formative assessment have underestimated the structural obstacles to pedagogical innovation within classrooms (Ruthven, 2009). This is not helped by a misinterpretation at a policy level of formative assessment as summative assessment in initiatives such as Assessing Pupil Progress (Black, 2009).

Research Questions

This paper will address the issue of how formative assessment can be implemented in mathematics education by examining the special case of algebra.

Methods

The approach has been developed collaboratively with a group of eight teachers using a design research methodology (e.g., Cobb et al, 2003). The paper will draw on analysis of semi-structured interviews with the teachers and evidence from classroom trials.

Frame

The paper will examine an approach to overcoming these difficulties using a series of research-based lessons in algebra that are being developed by the Increasing Competence and Confidence in Algebra and Multiplicative Structures (ICCAMS) project. The approach is informed by research on children’s methods (e.g., Plunkett, 1979; Hart, 1981; Küchemann, 1981), on previous teaching experiments involving diagnostic assessment (e.g., Bell, 1993) and on the design of curriculum materials (Remillard, Herbel-Eisenmann, & Lloyd, 2008).

Research findings

We discuss how a focus on the big ideas in school algebra (e.g., Watson, 2009) can support teachers’ subject knowledge whilst making the curriculum seem more manageable to teachers. In addition, we

consider ways in which the mathematical use of formative assessment may be exemplified and how a 'connectionist' approach to the teaching of mathematics may be encouraged (Askew et al, 1997). Finally, we suggest ways in which such an approach can be disseminated more widely. In particular, we discuss how curriculum guidance and textbooks might be better designed to facilitate more mathematically coherent and engaging teaching.

References

Askew, M., Brown, M., Rhodes, V., Johnson, D. C., & Wiliam, D. (1997). *Effective teachers of numeracy*. London: King's College.

Bell, A. (1993). Principles for the design of teaching. *Educational Studies in Mathematics*, 24(1), 5-34.

Black, P. J., Harrison, C., Lee, C., Marshall, B., & Wiliam, D. (2003). *Assessment for learning: putting it into practice*. Buckingham: Open University Press.

Black, P. J., & Wiliam, D. (1998). Assessment and classroom learning. *Assessment in Education*, 5(1), 7-73.

Black, P. (2009). Looking again at formative assessment. *Learning & Teaching Update*, 30(December 2009 / January 2010).

Cobb, P., Confrey, J., diSessa, A., Lehrer, R., & Schauble, L. (2003). Design experiments in educational research. *Educational Researcher*, 32(1), 9-13.

Haggarty, L., & Pepin, B. (2001). Mathematics textbooks and their use in English, French and German classrooms: a way to understand teaching and learning cultures. *Zentralblatt für Didaktik der Mathematik: International Reviews on Mathematical Education*, 33(5), 158-175.

Hart, K. (Ed.). (1981). *Children's understanding of mathematics: 11-16*. London: John Murray.

Hattie, J., & Timperley, H. (2007). The power of feedback. *Review of Educational Research*, 77(1), 81-112.

Hodgen, J. (2007). Formative assessment: tools for transforming school mathematics towards dialogic practice? In D. Pitta-Pantazi & G. Philippou (Eds.), *CERME 5: Fifth Congress of the European Society for Research in Mathematics Education* (pp. 1886-1895). Cyprus: European Society for Research in Mathematics Education, University of Cyprus.

Küchemann, D. E. (1981). *The understanding of generalised arithmetic (algebra) by secondary school children*. Unpublished PhD thesis, Chelsea College, University of London.

Plunkett, S. (1979). Decomposition and all that rot. *Mathematics in School*, 8(3), 2-5.

PricewaterhouseCoopers LLP. (2008). *Evaluation of the Making Good Progress Pilot. Interim Report. Research Report DCSF-RR065*. Nottingham: Department for Children, Schools and Families.

Remillard, J. T., Herbel-Eisenmann, B. A., & Lloyd, G. M. (Eds.). (2008). *Mathematics Teachers at Work: Connecting Curriculum Materials and Classroom Instruction*. London: Routledge.

Ruthven, K. (2009). Towards a naturalistic conceptualisation of technology integration in classroom practice: The example of school mathematics. *Education & Didactique*, 3(1), 131-152.

Smith, E., & Gorard, S. (2005). 'They don't give us our marks': the role of formative feedback in student progress. *Assessment in Education: Principles, Policy and Practice*, 12(1), 21-38.

Watson, A. (2006). Some difficulties in informal assessment in mathematics. *Assessment in Education*, 13(3), 289-303.

Watson, A. (2009). Paper 6: Algebraic reasoning. In T. Nunes, P. Bryant & A. Watson (Eds.), *Key understandings in mathematics learning*. London: Nuffield Foundation.